

## Supporting Information

### Ar chemistry

We follow the following types of particles: Ar neutral atoms in the ground state,  $e$  electrons,  $\text{Ar}^+$  ions,  $\text{Ar}_2^+$  molecular ions, and the excitation levels of 4s and 4p considered in the single lumped excitation levels: Ar(4s) and Ar(4p). The different collisions and radiative processes considered in the QN and PS models are presented in **Table SI.1** and **Table SI.2**.

Table SI.1. Electron-heavy particle collisions included in the QN and PS models.

Reaction	$E_{\text{th}}$ [eV]	Rate coefficient $k$ [ $\text{m}^3 \text{s}^{-1}$ ] <sup>a)</sup>	Reference
$e + \text{Ar} \rightarrow e + \text{Ar}$ , <i>elastic</i>	-	BOLSIG+ <sup>b)</sup>	[1]
$e + \text{Ar} \rightarrow e + \text{Ar}(4\text{s})$ , <i>excitation</i>	11.55	BOLSIG+	[1]
$e + \text{Ar}(4\text{s}) \rightarrow e + \text{Ar}$ , <i>de-excitation</i>	-11.55	BOLSIG+, DB <sup>c)</sup>	[1]
$e + \text{Ar} \rightarrow 2e + \text{Ar}^+$ , <i>direct ionization</i>	15.7	BOLSIG+	[1]
$e + \text{Ar}(4\text{s}) \rightarrow 2e + \text{Ar}^+$	4.15	BOLSIG+	[2]
$e + \text{Ar} \rightarrow e + \text{Ar}(4\text{p})$ , <i>excitation</i>	13	BOLSIG+	[1]
$e + \text{Ar}(4\text{p}) \rightarrow e + \text{Ar}$ , <i>de-excitation</i>	-13	BOLSIG+, DB	[1]
$e + \text{Ar}(4\text{p}) \rightarrow 2e + \text{Ar}^+$	2.8	BOLSIG+	[2]
$e + \text{Ar}(4\text{s}) \rightarrow e + \text{Ar}(4\text{p})$	1.08	BOLSIG+	[3]
$e + \text{Ar}(4\text{p}) \rightarrow e + \text{Ar}(4\text{s})$	-1.08	BOLSIG+, DB	[3]
$\text{Ar}^+ + 2e \rightarrow \text{Ar} + e$ , <i>3-body recombination</i>	-	$8.75 \times 10^{-39} (T_e(\text{eV}))^{-4.5} [\text{m}^6 \text{s}^{-1}]$	[4]
$\text{Ar}^+ + e + \text{Ar} \rightarrow \text{Ar} + \text{Ar}$	-	$1.5 \times 10^{-40} \left[ \frac{300}{T_g(\text{K})} \right]^{2.5} [\text{m}^6 \text{s}^{-1}]$	[5]
$e + \text{Ar}_2^+ \rightarrow \text{Ar}^+ + \text{Ar} + e$ , <i>electron impact</i>	-	$1.11 \times 10^{-12} \exp\left(-\frac{2.94 - 3(T_g(\text{eV}) - 0.026)}{T_e(\text{eV})}\right)$	[6]
$e + \text{Ar}_2^+ \rightarrow \text{Ar} + \text{Ar}(4\text{s})$	-	$1.04 \times 10^{-12} \left( \frac{300}{T_e(\text{K})} \right)^{0.67} \frac{1 - \exp[-418/T_g(\text{K})]}{1 - 0.31 \exp[-418/T_g(\text{K})]}$	[7, 8]

a) The rate coefficient for 3-body collisions has unit [ $\text{m}^6 \text{s}^{-1}$ ] and is explicitly mentioned where applicable; b) Boltzmann solver: the rate coefficients are calculated from the corresponding cross sections, based on solution of the Boltzmann equation with BOLSIG+[<sup>9</sup>]; c) Detailed balance (DB): the rate coefficients for the superelastic processes are calculated using the detailed balance principle[<sup>10</sup>] incorporated in BOLSIG+[<sup>9</sup>].

Table SI.2. Heavy particle-heavy particle collisions and radiative transitions included in the QN and PS models.

Reaction	Rate coefficient $k$ [ $\text{m}^3 \text{s}^{-1}$ ] / collision frequency $\nu_c$ [ $\text{s}^{-1}$ ]	Reference
$\text{Ar}(4s) + \text{Ar}(4s) \rightarrow \text{Ar}_2^+ + e$	$k = \frac{1}{2} 6.3 \times 10^{-16} \left[ \frac{300}{T_g(K)} \right]^{1/2}$	[11]
$\text{Ar}(4s) + \text{Ar}(4s) \rightarrow \text{Ar}^+ + \text{Ar} + e$	$k = 6.2 \times 10^{-16}$	[12]
$\text{Ar}^+ + 2\text{Ar} \rightarrow \text{Ar}_2^+ + \text{Ar}$	$k = 2.5 \times 10^{-43} \left( \frac{300}{T_g(K)} \right)^{3/2} [\text{m}^6 \text{s}^{-1}]$	[13]
$\text{Ar}_2^+ + \text{Ar} \rightarrow \text{Ar}^+ + 2\text{Ar}$	$k = \frac{6.06 \times 10^{-12}}{T_g(K)} \exp\left(-\frac{1.51 \times 10^4}{T_g(K)}\right)$	[6]
$\text{Ar}(4p) + \text{Ar} \rightarrow \text{Ar}(4s) + \text{Ar}$	$k = 5 \times 10^{-18}$	[13]
$\text{Ar}(4s) + \text{Ar}(4p) \rightarrow \text{Ar}^+ + \text{Ar} + e$	$k = 6.2 \times 10^{-16}$	[12]
$\text{Ar}(4p) + \text{Ar}(4p) \rightarrow \text{Ar}^+ + \text{Ar} + e$	$k = 6.2 \times 10^{-16}$	[12]
$\text{Ar}(4s) \rightarrow \text{Ar} + h\nu$	$\nu_c = g_{eff}^{b)} \times 3.145 \times 10^8$	[14]
$\text{Ar}(4p) \rightarrow \text{Ar}(4s) + h\nu$	$\nu_c = 4.4 \times 10^8$	[14]

a) The rate coefficient for 3-body collisions has unit [ $\text{m}^6 \text{s}^{-1}$ ] and is explicitly mentioned where applicable; b)  $g_{eff}$  depends on the characteristic dimension of the reactor and is calculated to be  $6 \times 10^4$  for the present reactor.[<sup>15</sup>]

In the QN model, the reaction rates for the  $\text{Ar}^+$ -Ar elastic isotropic scattering and scattering in backward direction (to simulate charge transfer) are calculated based on the momentum transfer

cross-sections.<sup>[16]</sup> In the PS model these rates are included in the calculation of the Ar<sup>+</sup> ion diffusion and mobility coefficients.<sup>[17]</sup>

## References

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